

# **Passive Sonar Tracking on Multibeam Intensities**

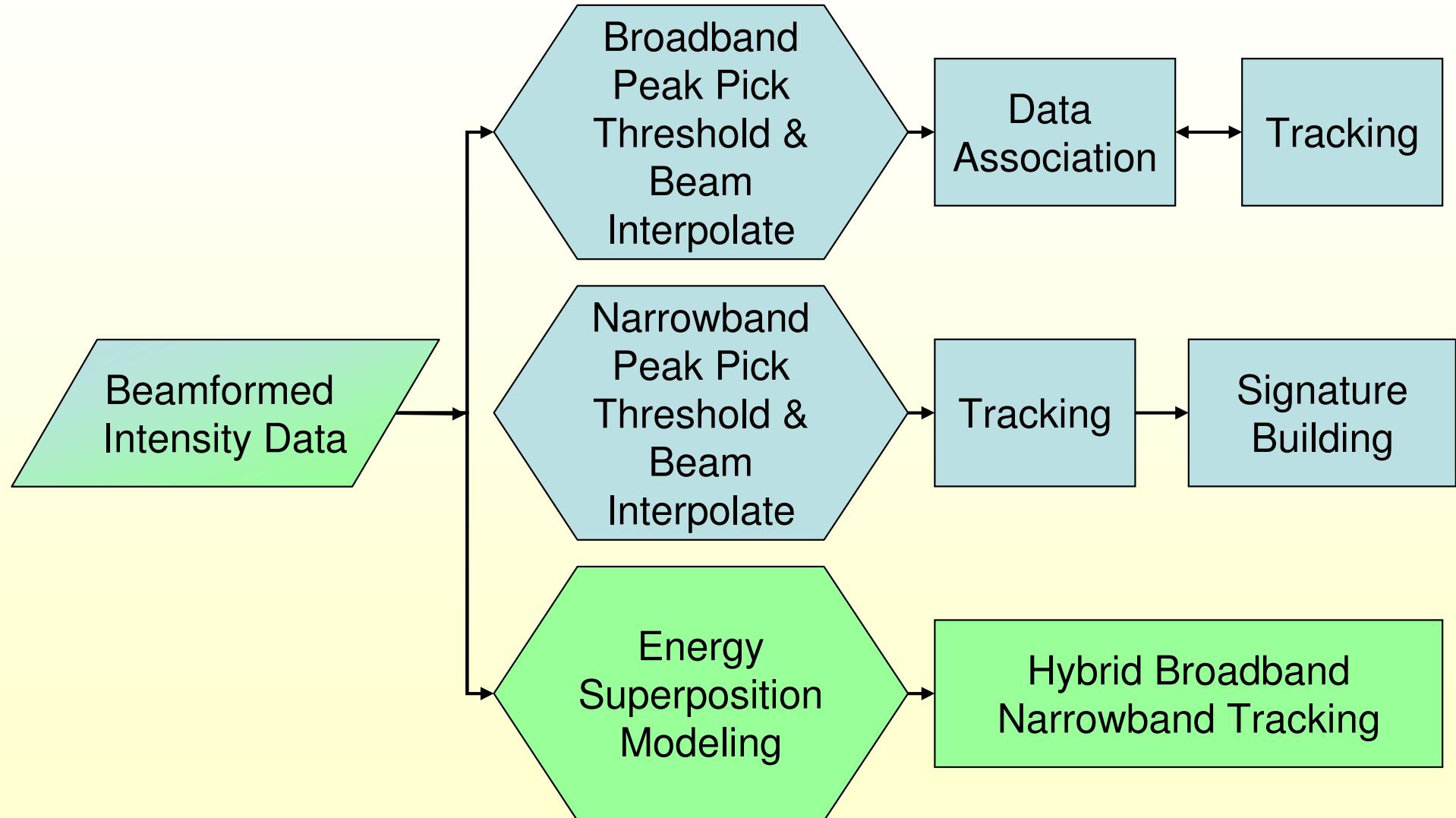
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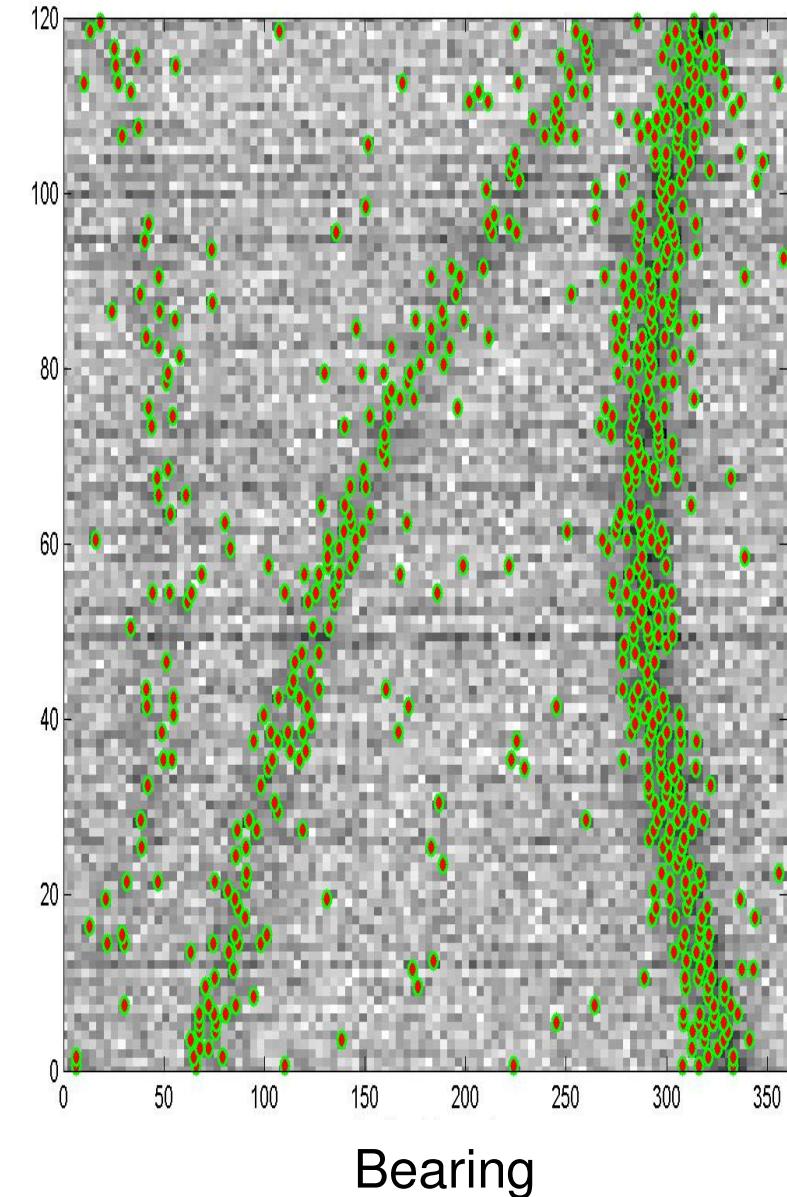
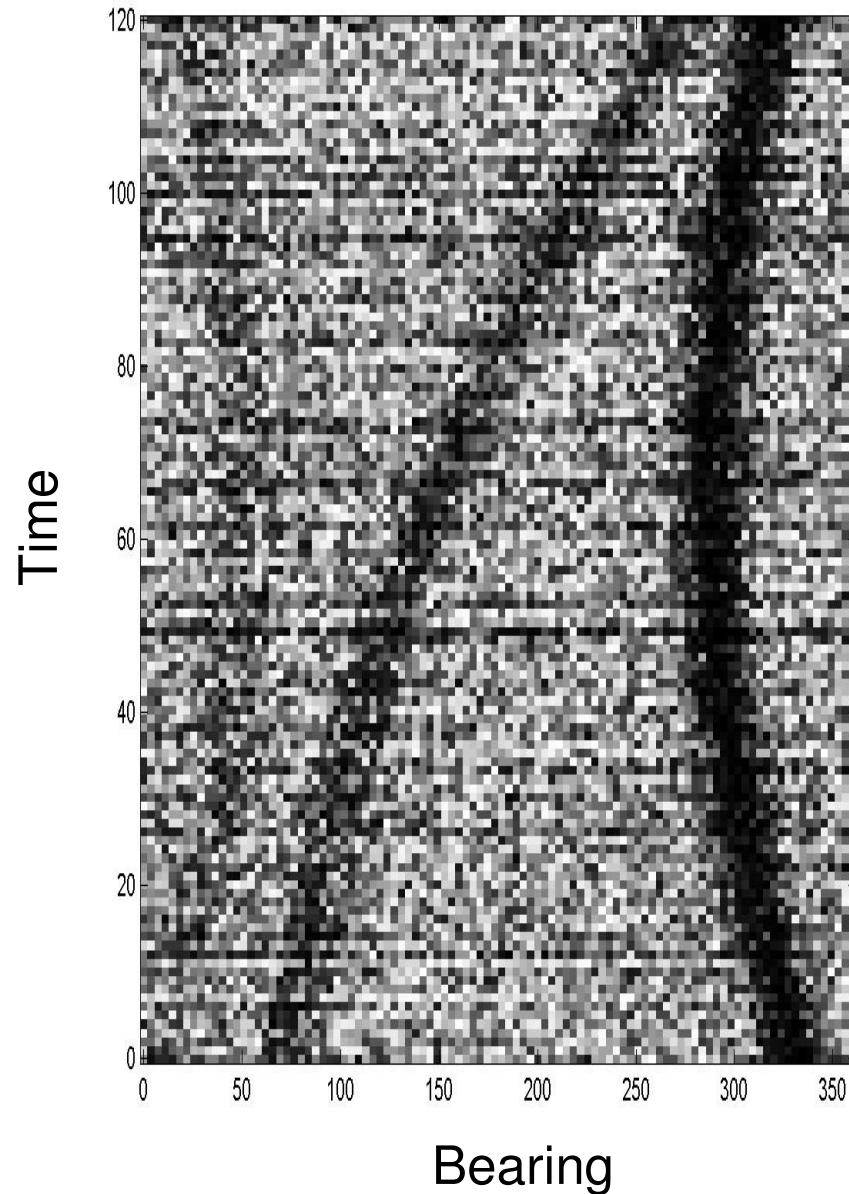
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# Sonar Processing Architectures



# Intensity Data

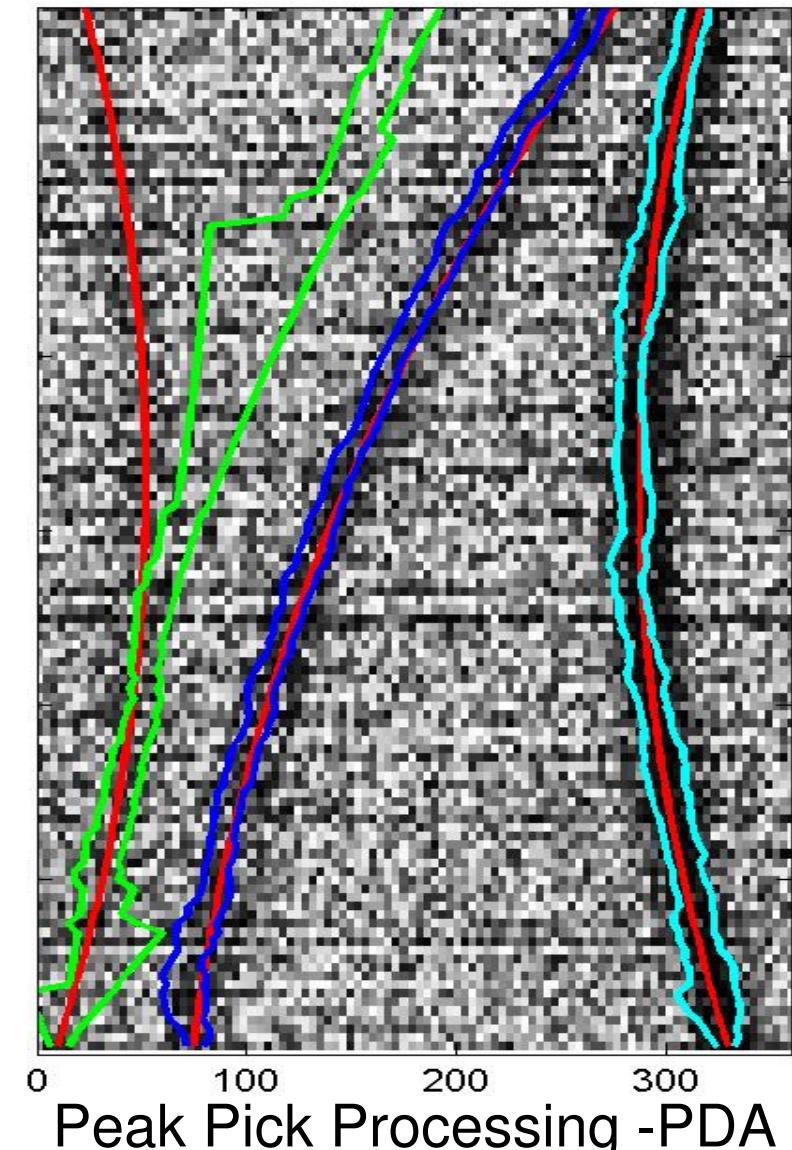
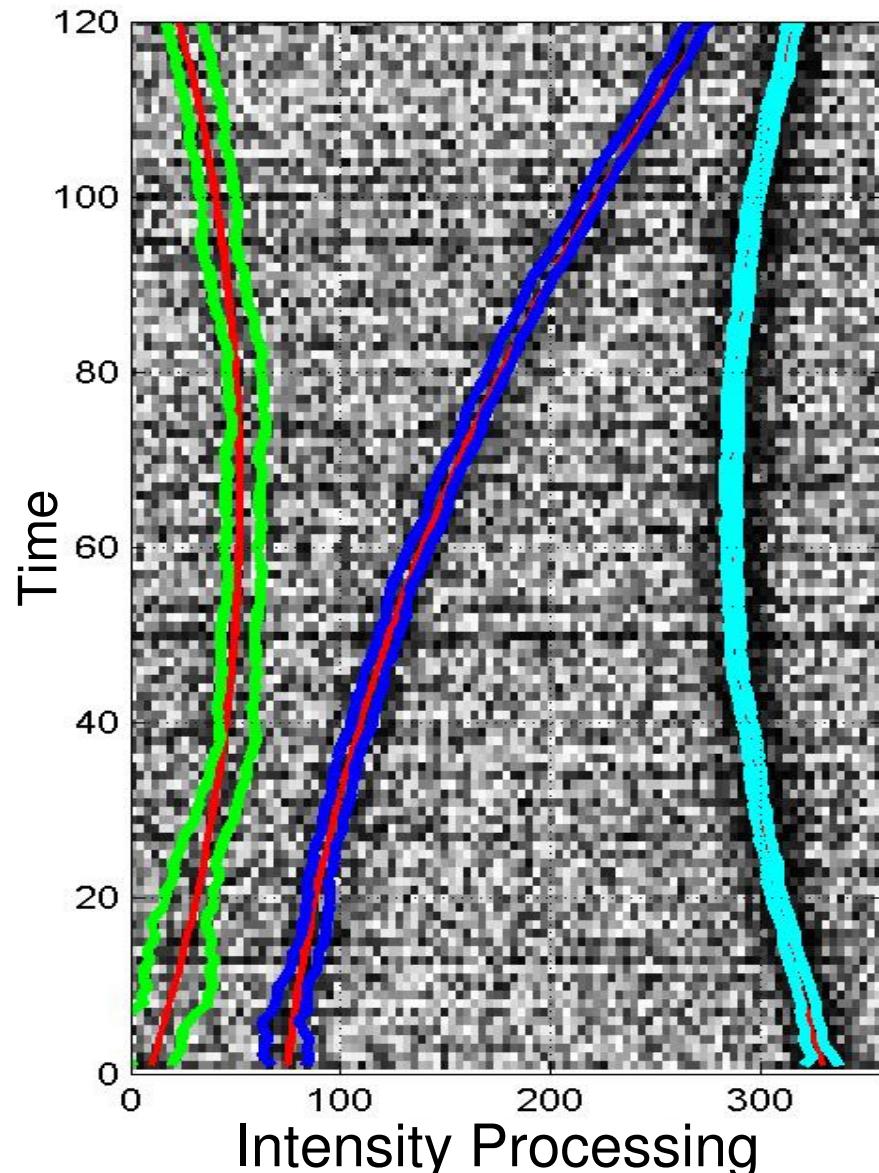
## Wide Targets, Increasing Intensity



# Single Target Tracking Results

## Wide Targets, Increasing Intensity

Estimated +/- 3 sigma overlaid on True Bearing



# History

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## Modeling multibeam intensity as a histogram

- **Perlovsky (c. 1991), Luginbuhl (c. 1999)**
  - Interpreted cell-level sensor data amplitudes as histogram counts
- **Streit (c. 2000), Streit (c. 2001)**
  - Treated broadband intensity as a histogram
  - Modeled the superposition of energy from multiple targets using a mixture density
  - Extended histogram interpretation to frequency-azimuth domain

## Direct energy superposition model

- **Ristic, Farina, Hernandez (c. 2004)**
  - Used a model of the sensor “point-spread function” to describe the distribution of energy across cells for tracking on image data
  - Applied a simple energy superposition model for developing a CRLB
  - No longer treating energy distribution as a pdf

# Basic Model

- The basic superposition model

$$\mathbf{Z}_t = \{z_{t,1}, z_{t,2}, \dots, z_{t,n}\}^T = C_t \mathbf{1}_n + \sum_{j=1}^k h(x_t^j) + \underline{\eta}_t$$

- The augmented state

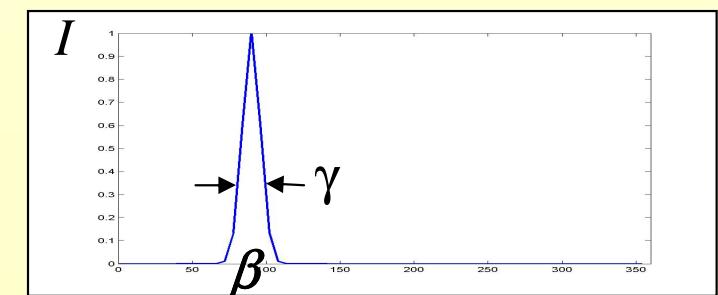
$$X_t = \{C_t, (x_t^1)^T, (x_t^2)^T, \dots, (x_t^k)^T\}^T$$

$$x_t^j = \{\beta_t^j, \dot{\beta}_t^j, I_t^j, \gamma_t^j\}^T$$

- The target viewed through the sensor point spread function

$$h(x_t^j) = \{h_1(x_t^j), h_2(x_t^j), h_3(x_t^j), \dots, h_n(x_t^j)\}^T$$

$$h_i(x_t^j) = I_t^j \exp \left\{ -\frac{1}{2} \frac{(\beta_i - \beta_t^j)^2}{\gamma_t^j} \right\}$$



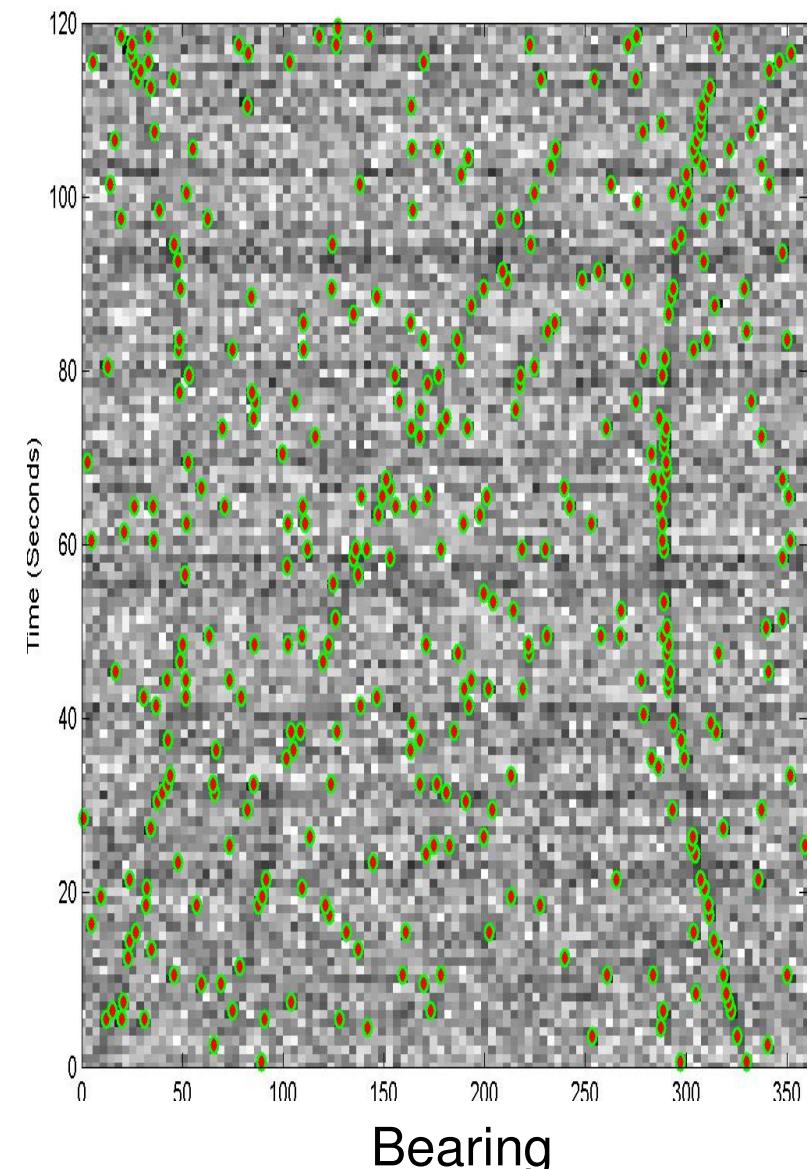
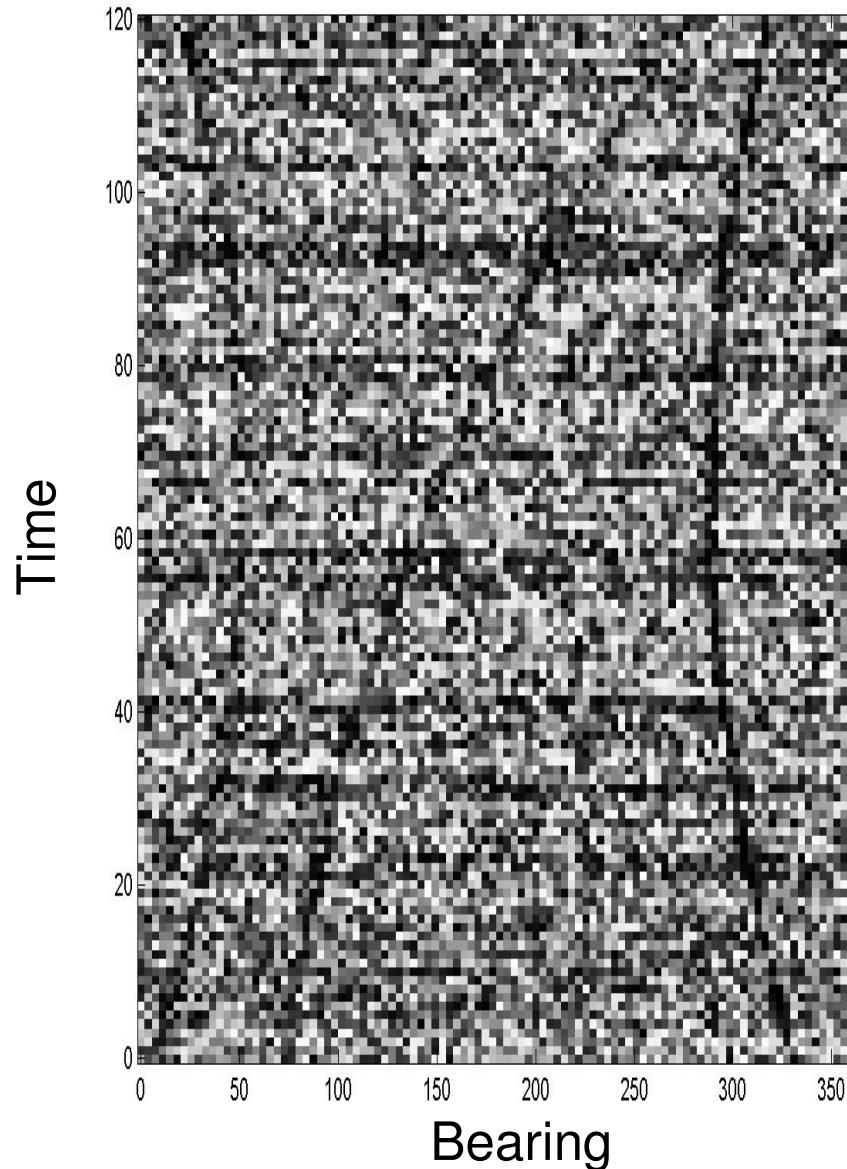
# Estimation Algorithm

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- **Non-Gaussian noise**
  - Not a problem for filtering, optimality sacrificed
  - Exponentially distributed frequency cells yield Gamma distributed broadband intensities, closely approximated by Gaussian
- **Applied straightforward Kalman filter**
  - Could use smoother, MLE or other
  - Relatively high dimensionality compared to traditional trackers
    - $n$ -vector measurement
    - $km+1$  vector state
- **Covariance decoupling**
  - If prior covariance is decoupled, so is much of the processing
  - Kalman gain can be performed with a  $km+1$  vs.  $n$  dimensional inversion
  - Output covariance is fully coupled, but little performance penalty seen from extracting target blocks to form a decoupled prior for the next update

# Intensity Data

## Narrow Targets, Increasing Intensity

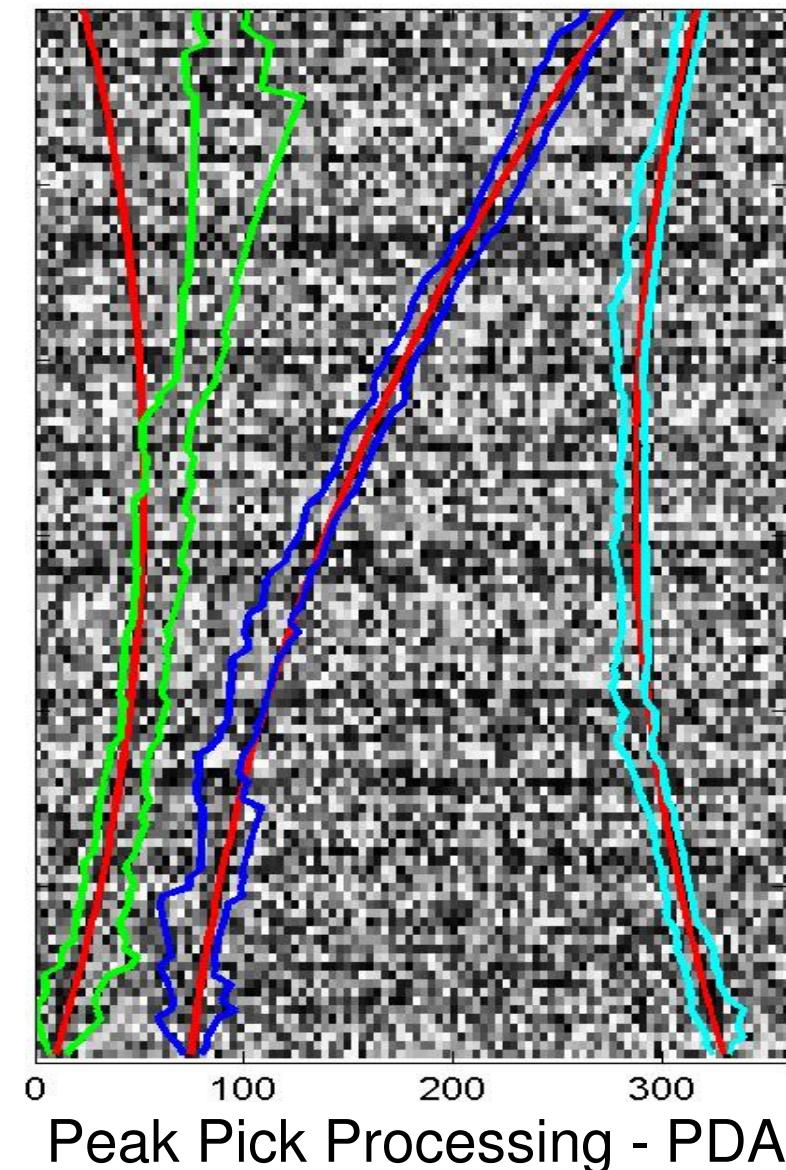
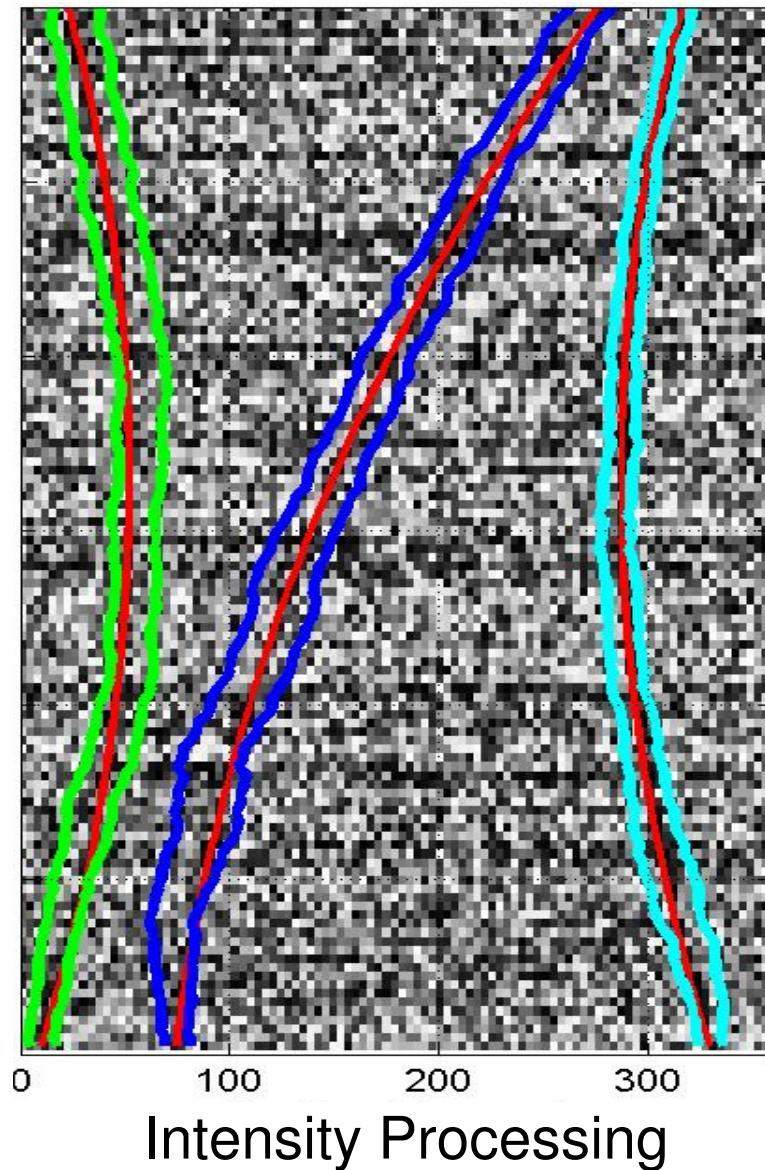


# Single Target Tracking Results

## Narrow Targets, Increasing Intensity

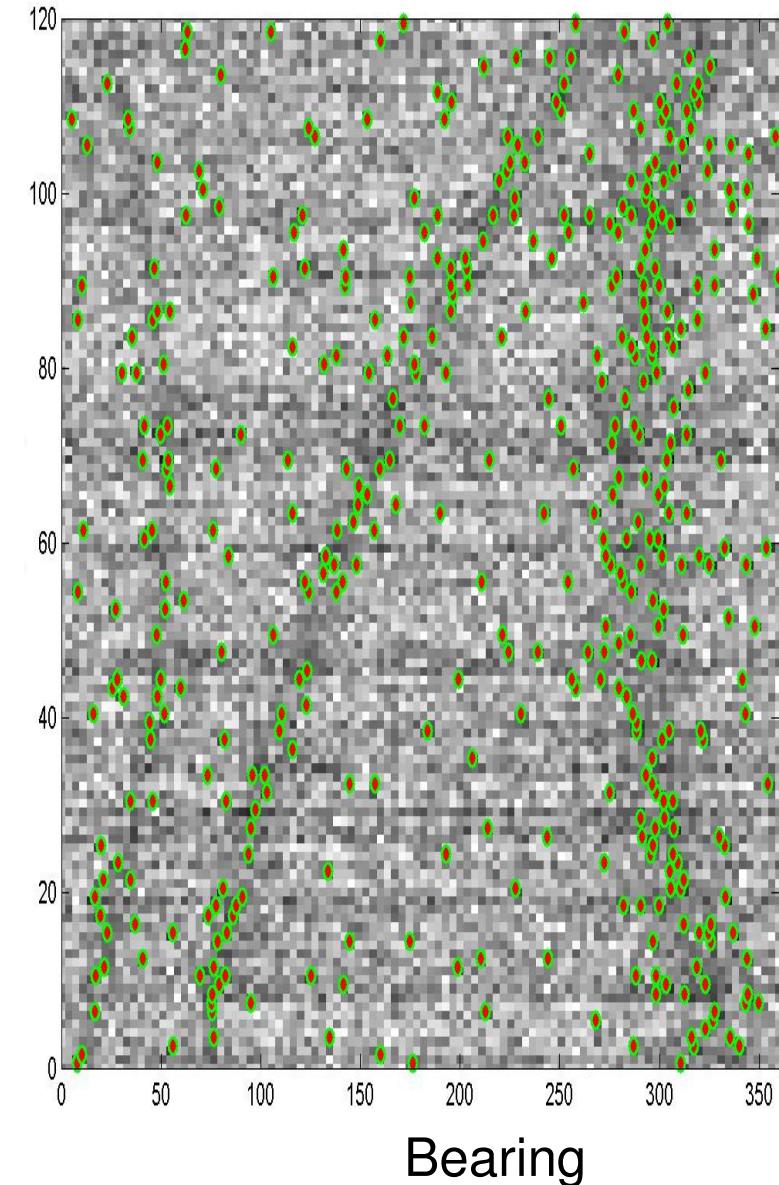
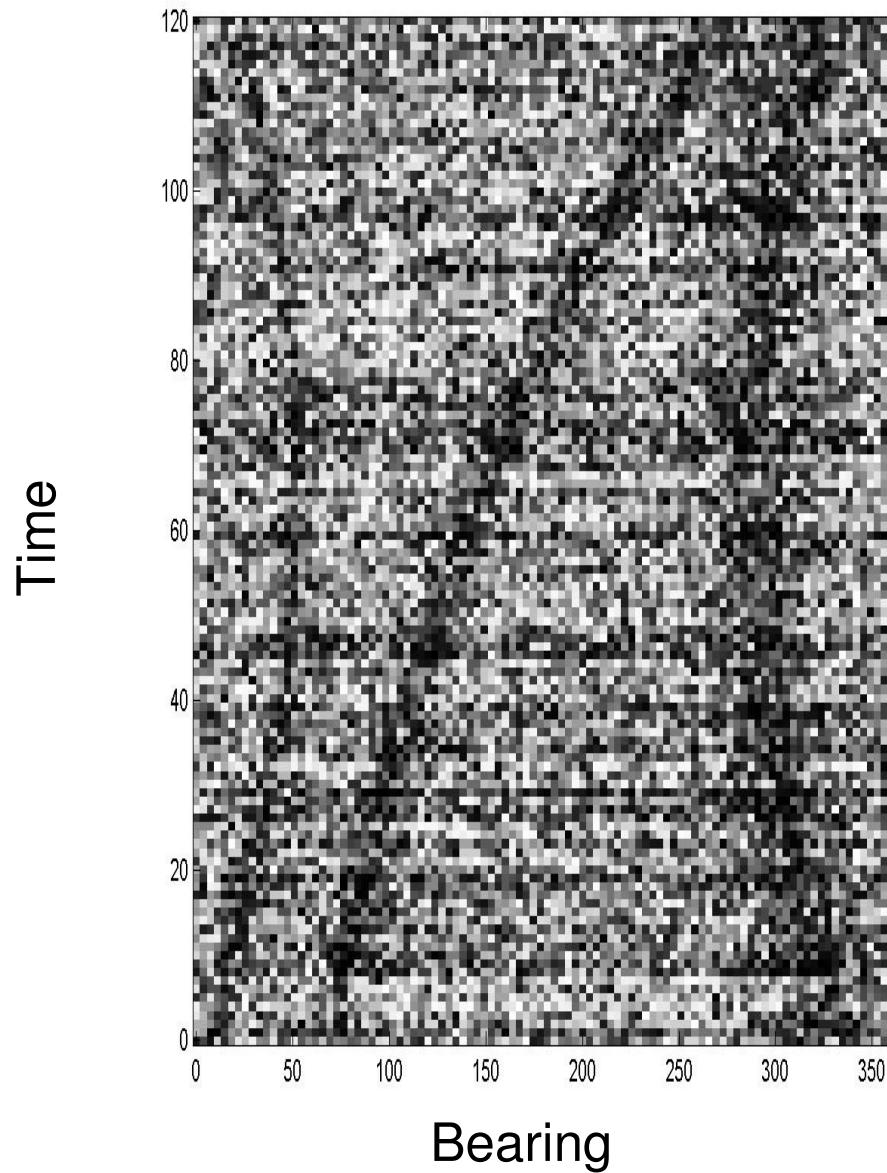
Estimated +/- 3 sigma overlaid on True Bearing

Time



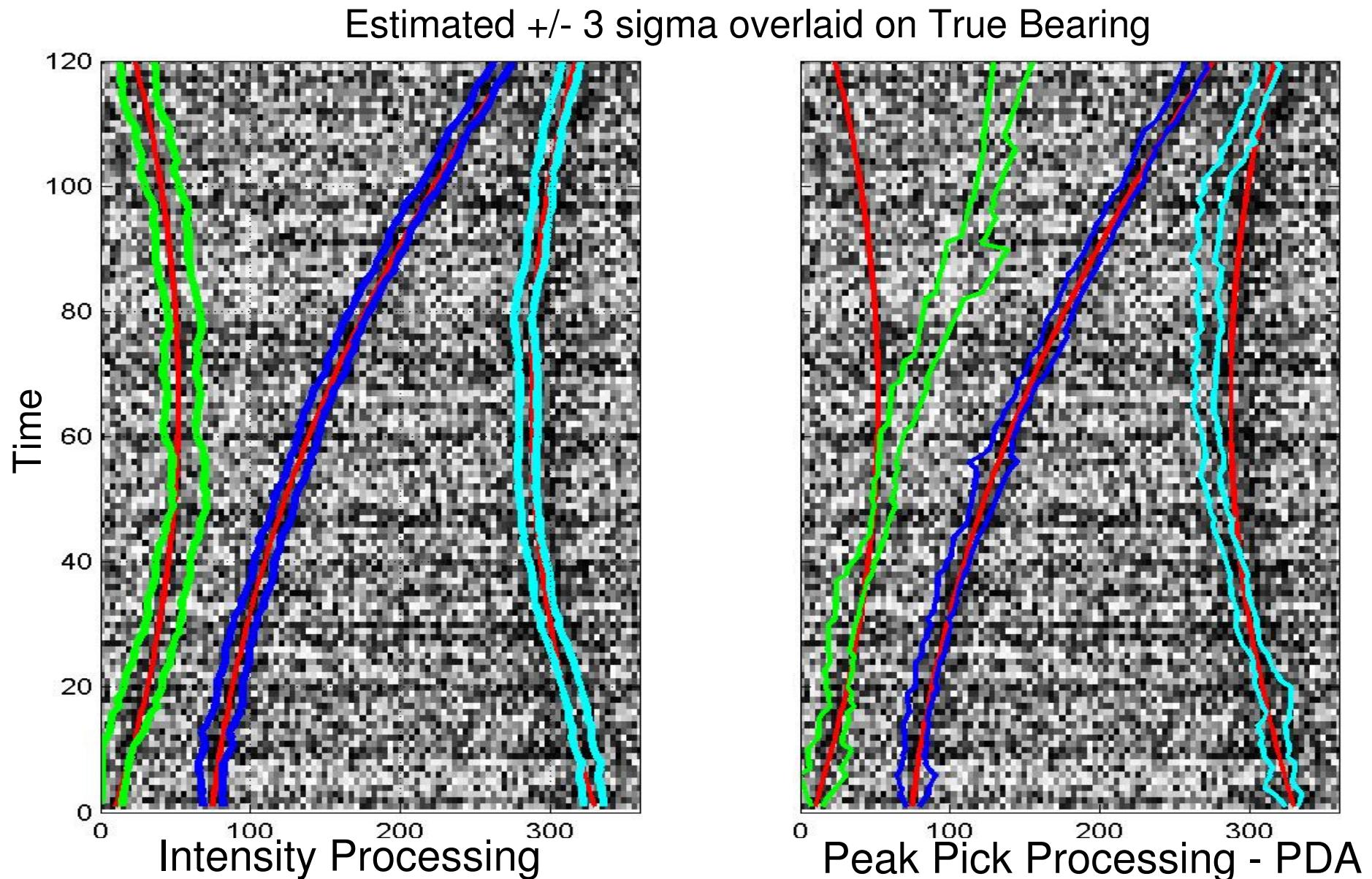
# Intensity Data

## Fixed Amplitude, Varying width Targets



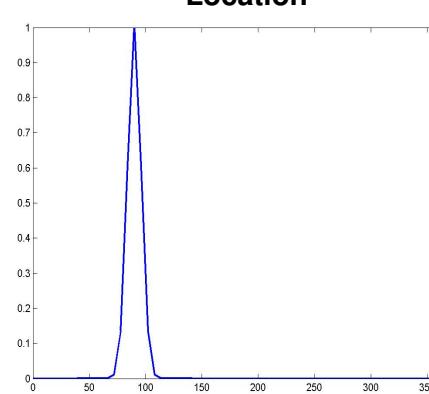
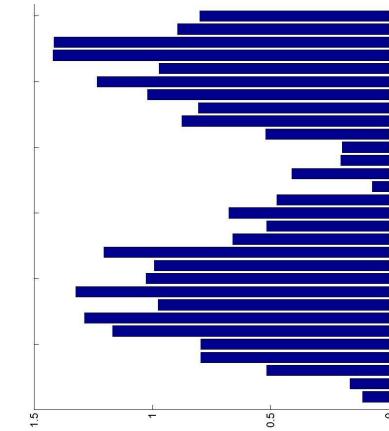
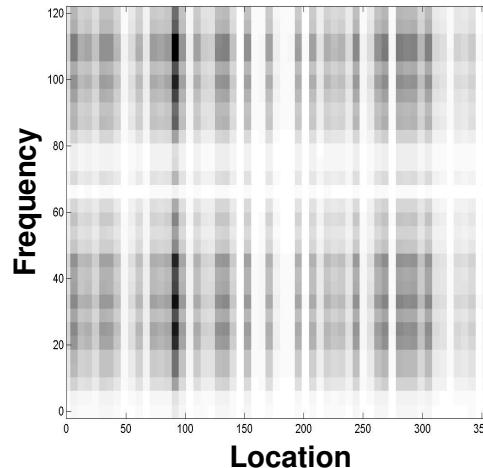
# Single Target Tracking Results

## Fixed Amplitude, Varying width Targets



# Improving SNR & Separability

**Data Scan**



**Parametric model of spatial location :**

$$h_i(x_t^j) = I_t^j \exp\left\{-\frac{1}{2} \frac{(\beta_i - \beta_t^j)^2}{\gamma_t^j}\right\}$$

**Non - parametric model of target spectral characteristics :**

$$S_t^j = \{s_{t,1}, s_{t,2}, \dots, s_{t,k}\}^T$$

**Outer product forms model of frequency - azimuth image :**

$$\text{FRAZ} = h_i(x_t^j)^T S_t^j$$

- Hold  $S^j$  fixed, estimate  $x^j$
- Given estimate of  $x^j$ , estimate  $S^j$  as a weighted average over beams, weighting based on  $h(x^j)$

# Summary

- Initialization requires detection, but tracking does not
- Superposition model results in an implicitly multitarget algorithm, no combinatorial problems
- Simple model admits simple processing
- Filter dimensionality is not a problem, simplifying approximations can make processing even simpler
- Provides reliable track bearing quality outputs
- “Self tuning”
- Tracks over-resolved targets without modification